



Proceedings of the fourteenth Congress of the European Society for Research in Mathematics Education

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